



**Marietta City Schools**  
**2023–2024 District Unit Planner**

*AP Calculus AB*

Unit title	Unit 5: Analytical Applications of Differentiation	Unit duration (hours)	3 weeks
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**Mastering Content and Skills through INQUIRY (Establishing the purpose of the Unit):** *What will students learn?*

**GA DoE Standards**

**Standards**

- 5.1 Using the mean value theorem
- 5.2 Extreme value theorem, global versus local extrema, and critical points
- 5.3 Determining intervals on which a function is increasing or decreasing
- 5.4 Using the first derivative test to determine relative (local) extrema
- 5.5 Using the candidates test to determine absolute (global) extrema
- 5.6 Determining concavity of functions over their domains
- 5.7 Using the second derivative test to determine extrema
- 5.8 Sketching graphs of functions and their derivatives
- 5.9 Connecting a function, its first derivative, and its second derivative
- 5.10 Introduction to optimization problems
- 5.11 Solving optimization problems
- 5.12 Exploring behaviors of implicit relations

**Concepts/Skills to support mastery of standards**

- Using the mean value theorem
- Extreme value theorem, global versus local extrema, and critical points
- Determining intervals on which a function is increasing or decreasing
- Using the first derivative test to determine relative (local) extrema
- Using the candidates test to determine absolute (global) extrema
- Determining concavity of functions over their domains
- Using the second derivative test to determine extrema
- Sketching graphs of functions and their derivatives
- Connecting a function, its first derivative, and its second derivative
- Introduction to optimization problems
- Solving optimization problems
- Exploring behaviors of implicit relations

### **Vocabulary**

Mean Value Theorem

Extreme Value Theorem

Global Extrema, Local Extrema

First Derivative Test

Concavity

Second Derivative Test

Optimization

it is safer and easier for students to make arguments about  $f$  based directly on the graph of the derivative, as in, " $f$  is concave up on  $a < x < b$  because the graph of  $f'$  is increasing on  $a < x < b$ ." Students should always refer to  $f$ ,  $f'$ , and  $f''$  by name, rather than by "it" or "the function," which may leave the reader unsure of their intended meaning.

### **Notation**

F', f'', and f with $dy/dx$ , $d^2y/dx^2$
<b>Essential Questions</b>
<p>How can calculus be used to verify certain aspects about a function?</p> <p>How can we use derivatives to understand the behavior of the graph of a function without the use of a graphing device?</p> <p>How is calculus used to find an optimal solution to a problem?</p>
<b>Assessment Tasks</b>
<i>List of common formative and summative assessments.</i>
<p><b><u>Formative Assessment(s):</u></b></p> <p>Skills Checks</p> <p>HW</p> <p>Quizzes</p> <p>Progress Checks in AP Classroom</p> <p><b><u>Summative Assessment(s):</u></b></p> <p>Unit Test</p>

<b>Learning Experiences</b> Add additional rows below as needed.		
Objective or Content	Learning Experiences	Personalized Learning and Differentiation
<b>5.8</b> <b>5.9</b>	Predict and Confirm  Provide students with the graph of a differentiable function, for example, $f(x) = x^4 + 4x^3 - 12x^2 + 32x - 1$	Collaborative groups and extension on AP classroom

	<p>++ , but do not provide the rule for the function. Ask students to sketch a graph of the derivative of the function. Once students are done, reveal the rule for <math>f(x)</math>. Ask students to calculate <math>f'(x)</math>, and use technology to graph <math>f'(x)</math> and compare it to their sketched graph.</p>	
<p><b>Content Resources</b></p>		
<ul style="list-style-type: none"> <li>• AP Classroom (within AP Central, collegeboard.org)</li> <li>• Calculus textbook: Calculus, 11e, Larson &amp; Edwards</li> <li>• Tony Record (Avon HS) created resources</li> <li>• Khan Academy</li> <li>• Delta Math</li> <li>• Master Math Mentor (pdf files and videos)</li> <li>• Teacher created resources</li> </ul>		